

Reglas de derivación

Suma

$$y = u + v \quad y' = u' + v'$$

Resta

$$y = u - v \quad y' = u' - v'$$

Producto

$$y = u v \quad y' = u' v + v' u$$

Cociente

$$y = \frac{u}{v} \quad y' = \frac{u' v - v' u}{v^2}$$

$$y = k \quad y' = 0$$

$$y = x \quad y' = 1$$

$$y = k x \quad y' = k$$

$$y = \frac{1}{x} \quad y' = \frac{-1}{x^2}$$

$$y = x^2 \quad y' = 2x$$

$$y = x^n \quad y' = n x^{n-1}$$

$$y = e^x \quad y' = e^x$$

$$y = a^x \quad y' = a^x \ln a$$

$$y = \ln x \quad y' = \frac{1}{x}$$

$$y = \log_a x \quad y' = \frac{1}{x \ln a}$$

$$y = \sqrt{x} \quad y' = \frac{1}{2\sqrt{x}}$$

$$y = \operatorname{sen} x \quad y' = \cos x$$

$$y = \cos x \quad y' = -\operatorname{sen} x$$

$$y = \tan x \quad \begin{cases} y' = 1 + \tan^2 x \\ = \frac{1}{\cos^2 x} = \sec^2 x \end{cases}$$

$$y = \cot x \quad y' = \frac{-1}{\operatorname{sen}^2 x} = -\operatorname{cosec}^2 x$$

$$y = \arcsen x \quad y' = \frac{1}{\sqrt{1-x^2}}$$

$$y = \arccos x \quad y' = \frac{-1}{\sqrt{1-x^2}}$$

$$y = \arctan x \quad y' = \frac{1}{1+x^2}$$

$$y = u \quad y' = u'$$

$$y = k u \quad y' = k u'$$

$$y = \frac{1}{u} \quad y' = \frac{-u'}{u^2}$$

$$y = u^2 \quad y' = 2u u'$$

$$y = u^n \quad y' = n u^{n-1} u'$$

$$y = e^u \quad y' = u' e^u$$

$$y = a^u \quad y' = u' a^u \ln a$$

$$y = \ln u \quad y' = \frac{u'}{u}$$

$$y = \log_a u \quad y' = \frac{u'}{u \ln a}$$

$$y = \sqrt{u} \quad y' = \frac{u'}{2\sqrt{u}}$$

$$y = \operatorname{sen} u \quad y' = u' \cos u$$

$$y = \cos u \quad y' = -u' \operatorname{sen} u$$

$$y = \tan u \quad \begin{cases} y' = (1 + \tan^2 u) u' \\ = \frac{u'}{\cos^2 u} = u' \sec^2 u \end{cases}$$

$$y = \cot u \quad y' = \frac{-u'}{\operatorname{sen}^2 u} = -u' \operatorname{cosec}^2 u$$

$$y = \arcsen u \quad y' = \frac{u'}{\sqrt{1-u^2}}$$

$$y = \arccos u \quad y' = \frac{-u'}{\sqrt{1-u^2}}$$

$$y = \arctan u \quad y' = \frac{u'}{1+u^2}$$

Derivación logarítmica

$$1) \quad y = u^v$$

$$2) \quad \ln y = \ln(u^v)$$

$$3) \quad \ln y = v \ln u$$

$$4) \quad \frac{y'}{y} = v' \ln u + v \frac{u'}{u} \quad 5) \quad y' = y \left(v' \ln u + v \frac{u'}{u} \right) \quad 6) \quad y' = u^v \left(v' \ln u + v \frac{u'}{u} \right)$$

Siendo: y, u, v funciones de x ; a, k, n constantes.